

# Algorithmic Game Theory: from Multi-agent Optimization to On-line Learning

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# Motivation & Outline

You are planning your commute route for tomorrow.

Not sure about your departure time, nor who might be on the road.



**A game with a random set of players !**

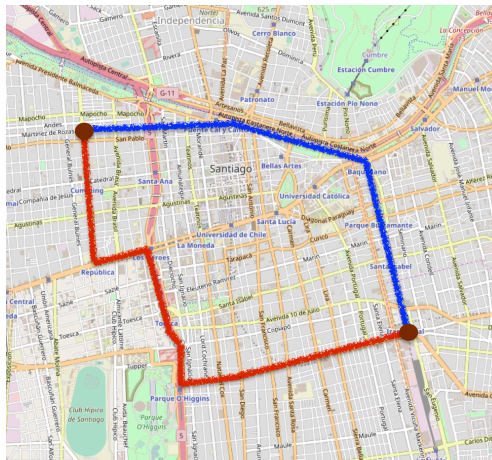
**In US alone, congestion cost US\$305 billion in 2017**  
 **$\approx 1.6\%$  of GNP... 3% increase from previous year !**

(source: INRIX)

Lost productivity of workers sitting in traffic, wasted fuel...

...before accounting for environmental impacts, accidents, quality of life.

# Urban traffic under congestion



2266 nodes / 7636 arcs

## SANTIAGO

6.000.000 people  
11.000.000 daily trips  
1.750.000 car trips

## Morning peak

500.000 car trips  
29.000 OD pairs

# Many Questions

- ① How should we model traffic and congestion ?
  - Urban traffic / transit systems / telecom / logistic networks
  - Selfish routing / routing apps / autonomous vehicles
- ② Equilibrium models vs adaptive dynamics ?
  - Can players “*learn*” how to play an equilibrium ?
  - Informational constraints and bounded rationality
- ③ Deterministic or stochastic models ?
  - What are the impacts of uncertainty and risk-aversion ?
- ④ Static vs dynamic routing ?
- ⑤ Asymptotics for large games ?
- ⑥ How inefficient is selfish routing ?
  - How (much) can we reduce congestion ?

...and more !

# Outline of the Mini-course

## Part I (Cominetti)

- **Lecture 1:** Basic concepts in game theory
- **Lecture 2:** Non-atomic routing games – Wardrop equilibrium
- **Lecture 3:** Large routing games – Wardrop or Poisson?

## Part II (Mertikopoulos)

- **Lecture 4:** Game dynamics and evolutionary biology
- **Lecture 5:** Learning in finite games and multi-armed bandits
- **Lecture 6:** Learning in continuous games and online convex optimization